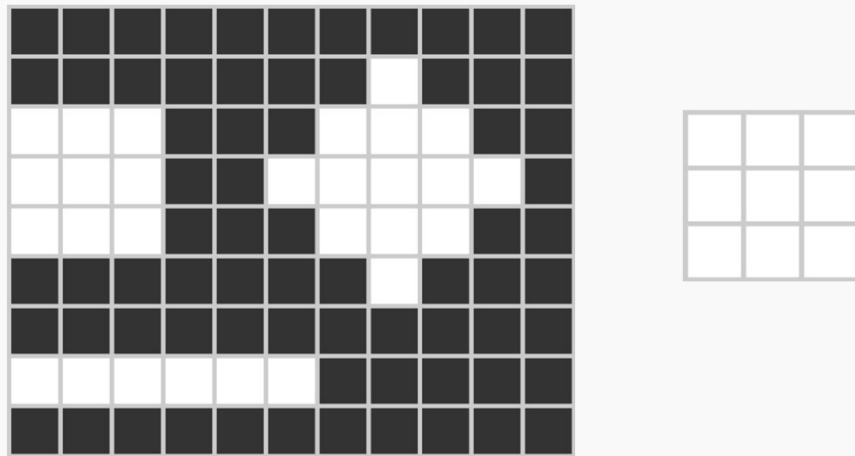


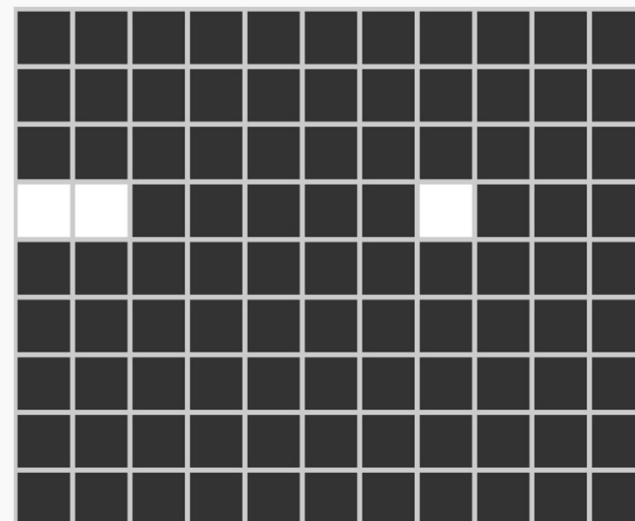
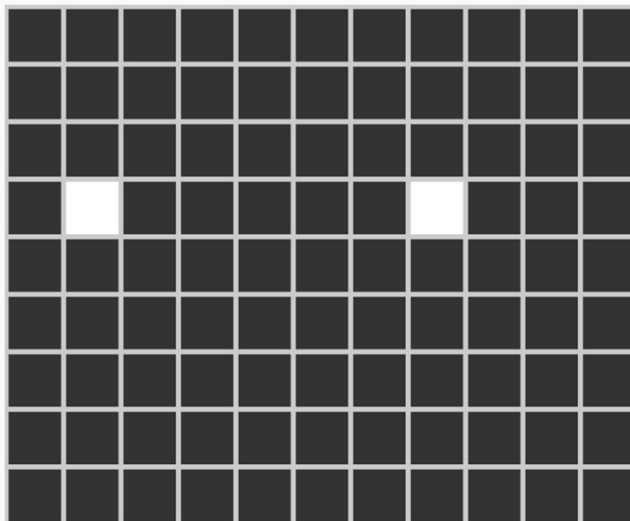
MATLAB Lecture 8: Plots and curve fitting

MCDB/BCHM 4312/5312

Homework 6: Erosion in MATLAB

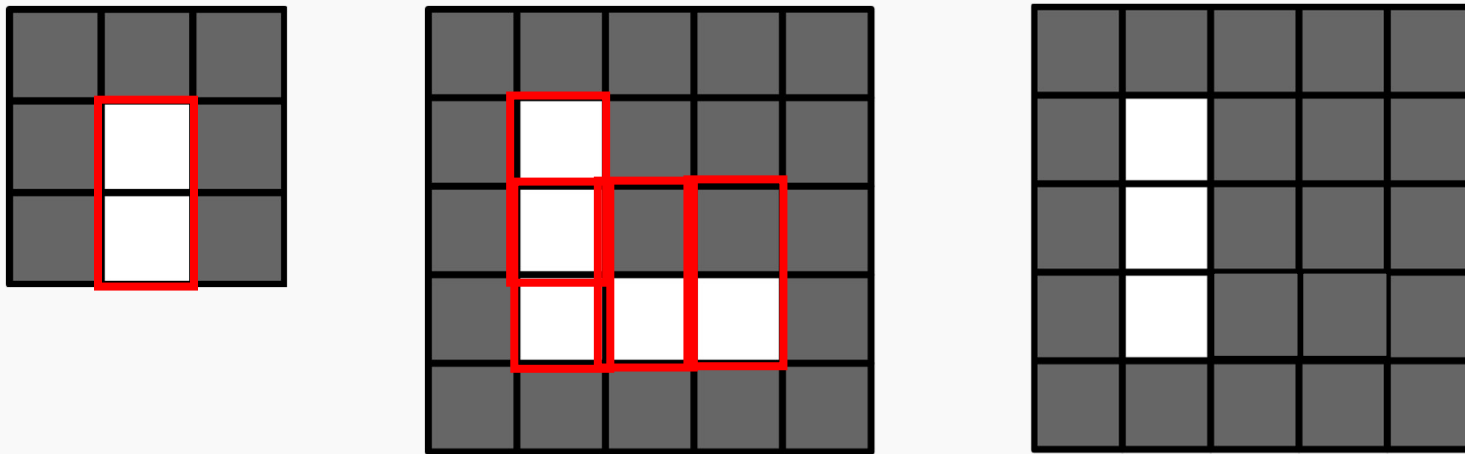


Both these answers are correct



This is how MATLAB treats the edges ²

Lecture 5: Morphological opening

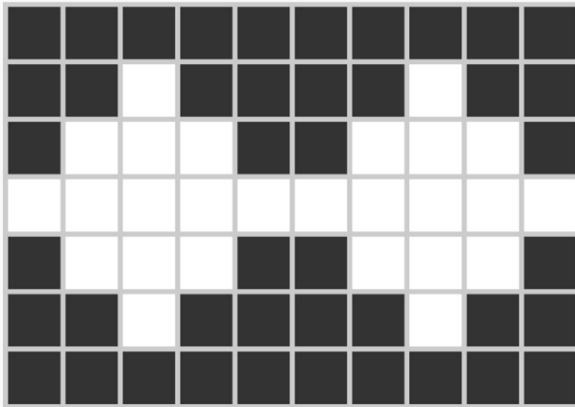


Slide the structuring element over all the foreground pixels

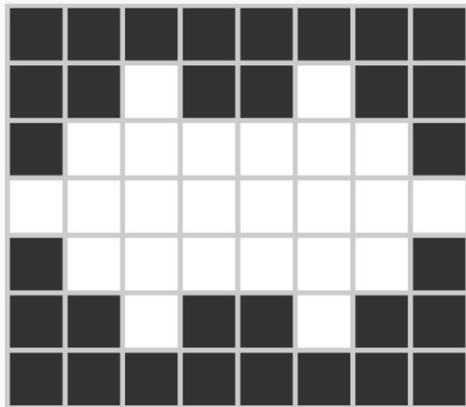
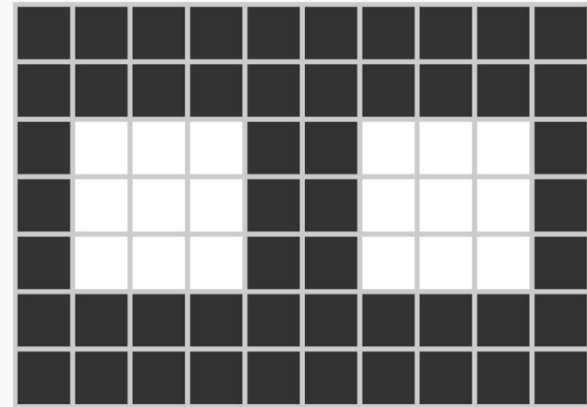
All pixels in the image which fits the structuring element will be kept

Homework 6: Morphological opening

- Actually quite difficult to separate objects with an opening
 - Only works if objects were minimally connected to being with



You could separate these using a [1 1] structuring element



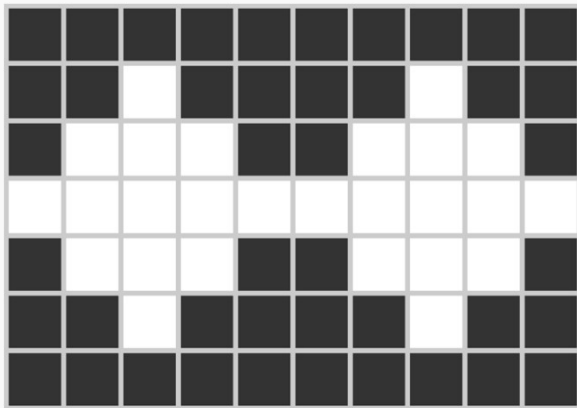
Would be much harder to separate these objects

Watershed is a better approach for separating objects

Example code to test

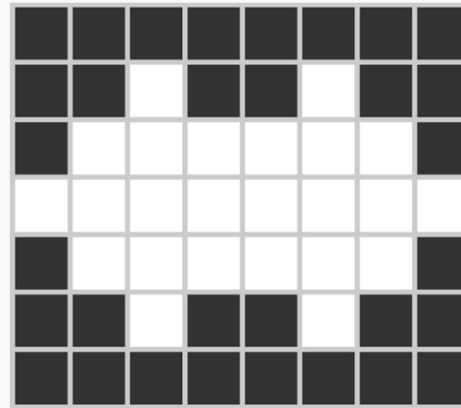
```
M = [0 0 1 0 0 0 0 1 0 0;  
      0 1 1 1 0 0 1 1 1 0;  
      1 1 1 1 1 1 1 1 1 1;  
      0 1 1 1 0 0 1 1 1 0;  
      0 0 1 0 0 0 0 1 0 0];
```

```
imopen(M, ones(2))
```

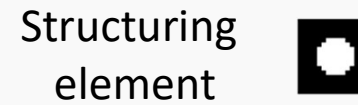


```
M = [0 0 1 0 0 1 0 0;  
      0 1 1 1 1 1 1 0;  
      1 1 1 1 1 1 1 1;  
      0 1 1 1 1 1 1 0;  
      0 0 1 0 0 1 0 0];
```

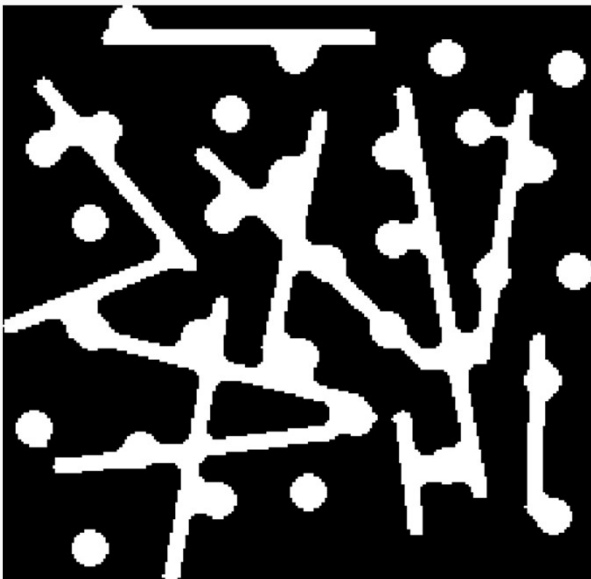
```
imopen(M, ones(2))
```



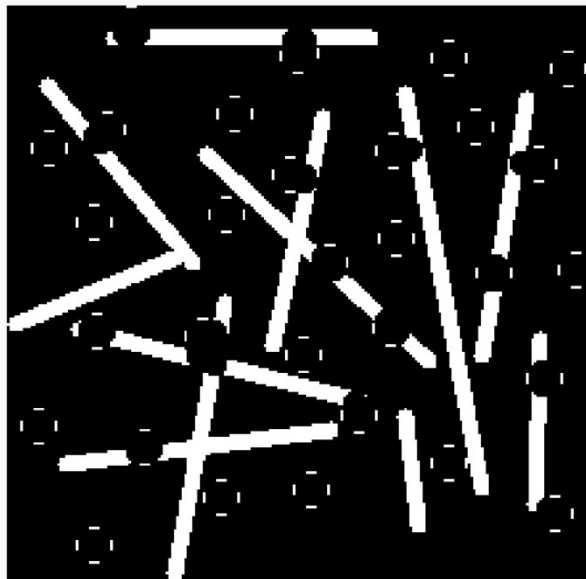
What is the result of the morphological opening operation?



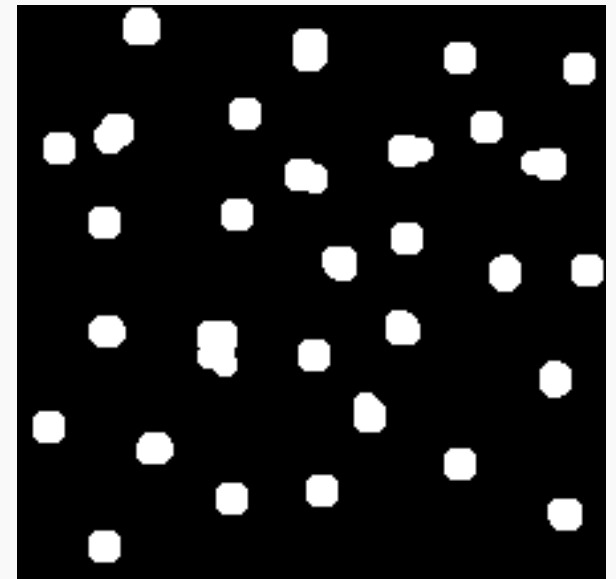
(A)



(B)



(C)



Useful applications of opening

- Removing unwanted shapes
 - Tidying up boundaries of segmented cells
 - Removing contamination/unwanted objects
- Removing small objects – opening removes objects smaller than the structuring element

Learning Goals

- How to plot data in MATLAB
- Curve fitting
- Interpolating data

How to plot your data

Basic line plot syntax:

```
plot(xdata, ydata)
```

xdata and ydata must have the same lengths

Creating a range of values

- Remember the colon operator can provide you with a vector of numbers

```
xdata = 1:10
```

- You can also specify a step size

```
xdata = 1:2:10
```

Note: the colon operator will not include the last point if it does not line up with the step size

```
xdata = [1, 3, 5, 7, 9]
```

Another way of creating a range of values

Syntax:

```
xdata = linspace(start, end, number of points)
```

- linspace = **linear space**
- Unlike the colon operator, `linspace` will include both the start and end values

Example

Write a script to do the following:

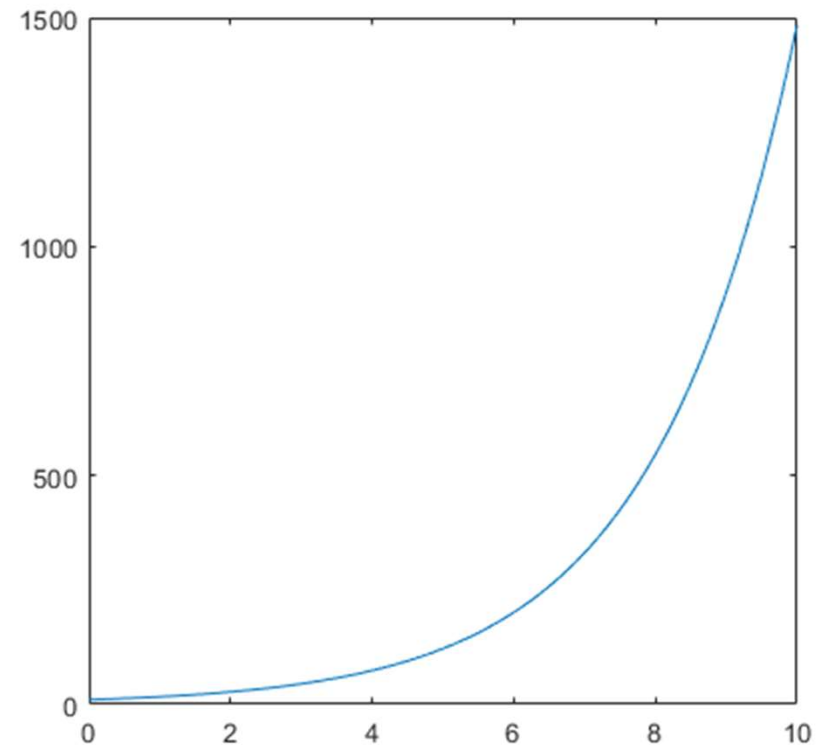
1. Create a linearly spaced array ranging from [0, 10] with 100 points called xdata
2. Evaluate the following function over xdata

$$y = 10e^{0.5x}$$

3. Plot the data using a line plot

```
plot(xdata, ydata)
```

```
xx = linspace(0, 10, 100);  
yy = 10 * exp(0.5 * xx);  
plot(xx, yy)
```



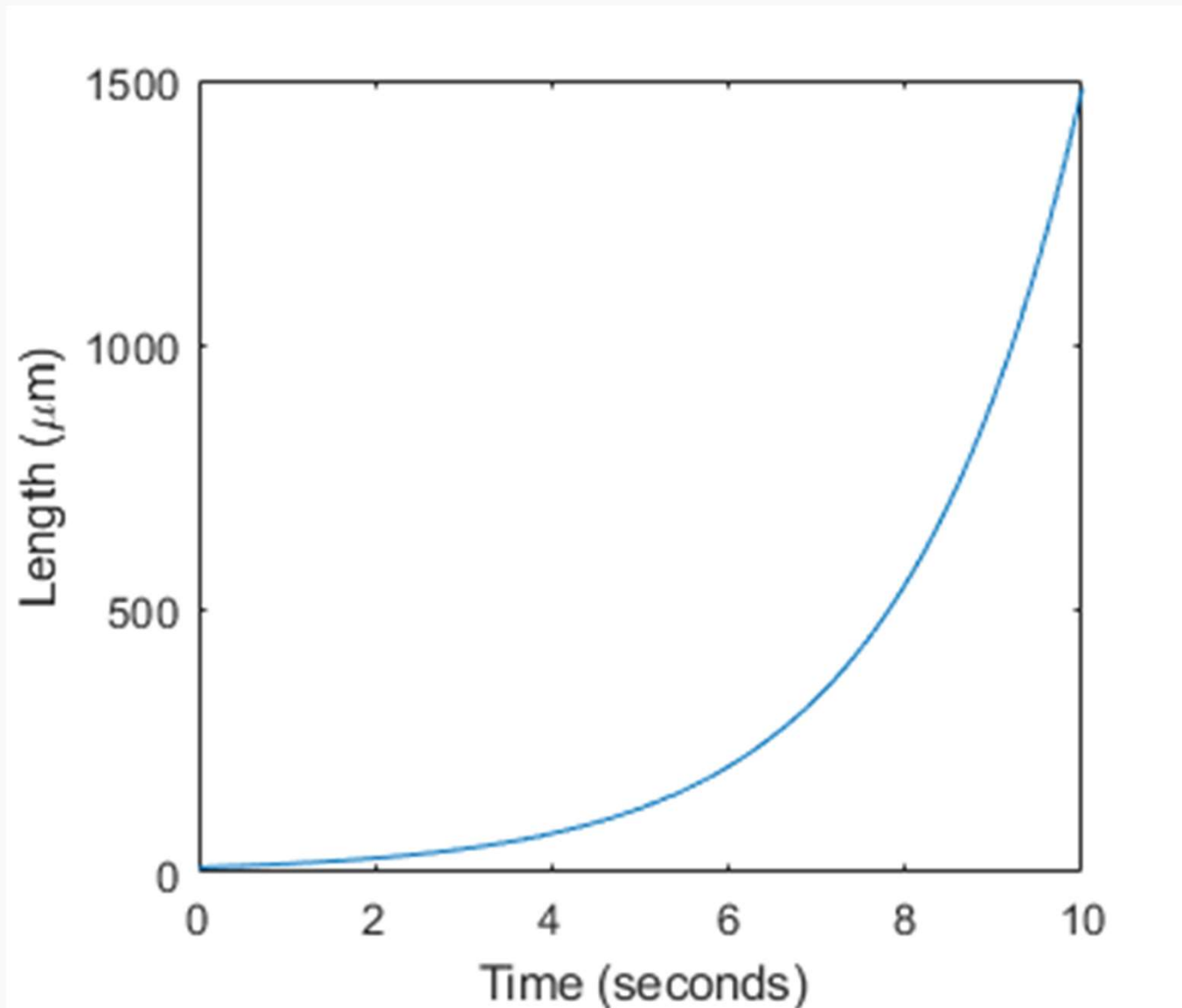
Labeling your axes

- Hopefully everyone recognized that the equation was for exponential growth
 - E.g. bacteria length, number of cells
- Label the axes as:

```
xlabel('Time (seconds)')
```

```
ylabel('Length (\mum)')
```

Labeled axes



Axes and title labels

- By default, MATLAB will interpret TeX/LaTeX style commands
- Examples for Greek letters:

`\mu`

`\theta`

`\Theta`

- Examples for subscript and superscripts: `_` and `^`
- Full list:
https://www.mathworks.com/help/matlab/creating_plots/greek-letters-and-special-characters-in-graph-text.html

Axes and title labels

- To disable this behavior, specify additional arguments:

```
ylabel('Length \mum', 'Interpreter', 'none')
```



Length \mum

Titles

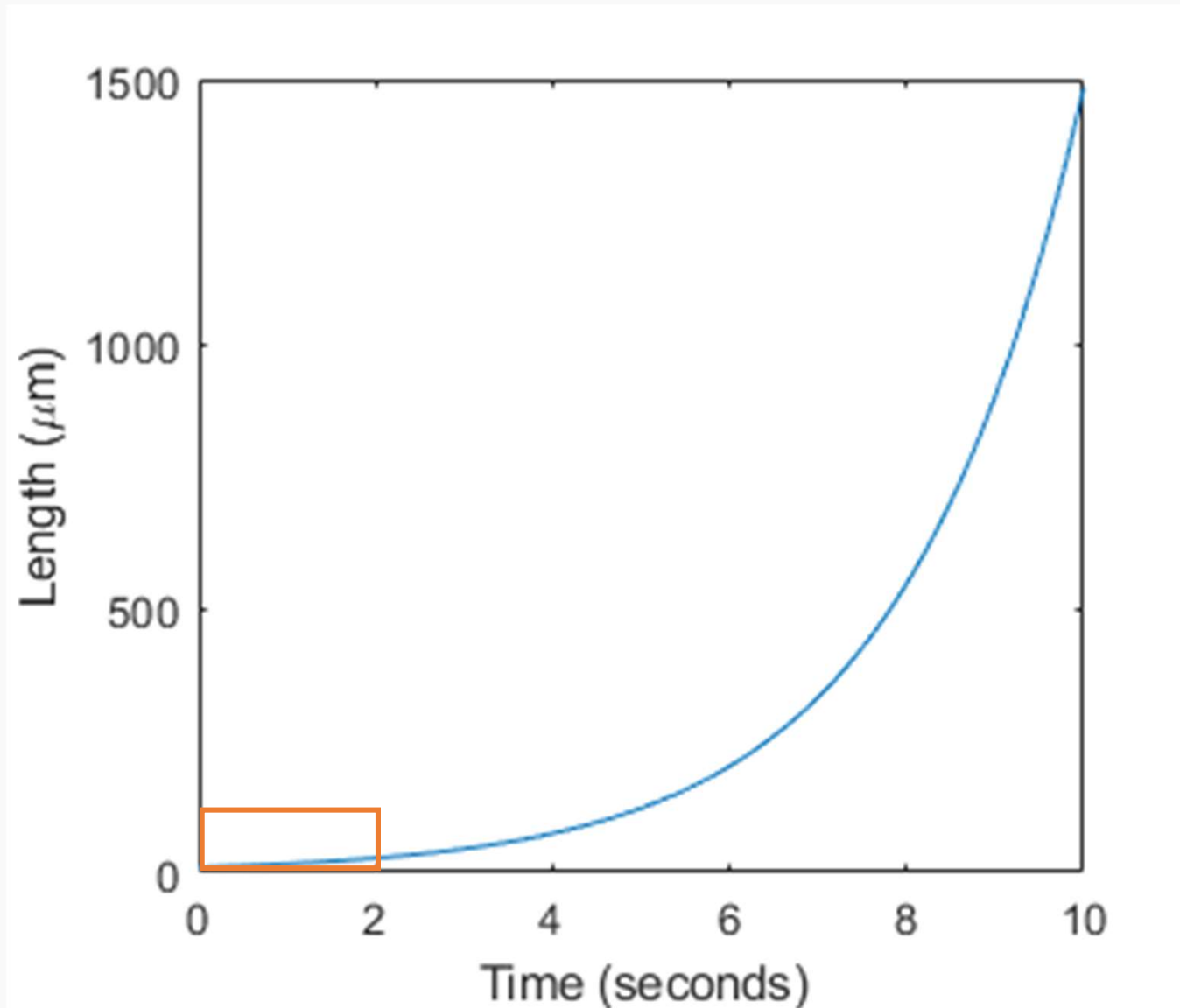
- You can add titles using the command

```
title('Bacterial growth')
```

One small detail

- Most figure commands (e.g. `title`, `xlabel`, `plot`) will operate on the last selected figure
- Last selected figure =
 - Last figure that was created, or
 - Last figure window that you selected
- To select a figure programmatically, you can use `figure(number)`
- E.g. `figure(1)` selects the window titled Figure 1

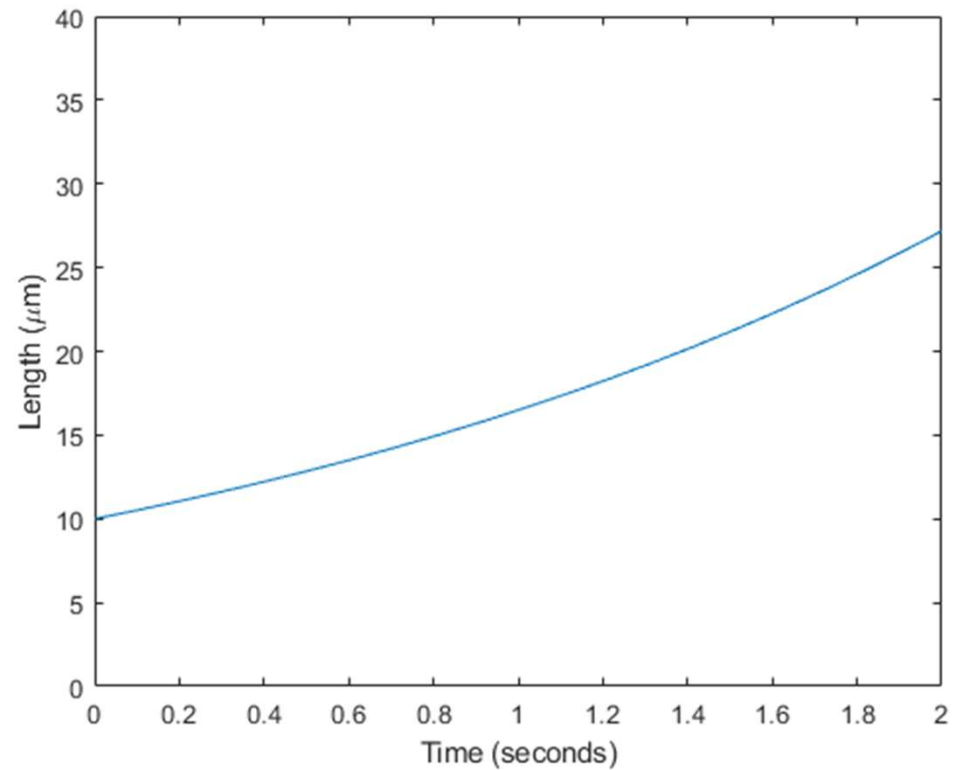
Specifying limits for the axes



Specifying limits for the axes

After plotting:

```
xlim([0, 2])  
ylim([0, 40])
```



Example code

```
xx = linspace(0, 10, 100);  
yy = 10 * exp(0.5 * xx);  
  
plot(xx, yy)  
xlabel('Time (seconds)');  
ylabel('Length (\mum)');  
xlim([0, 2])  
ylim([0, 40])
```

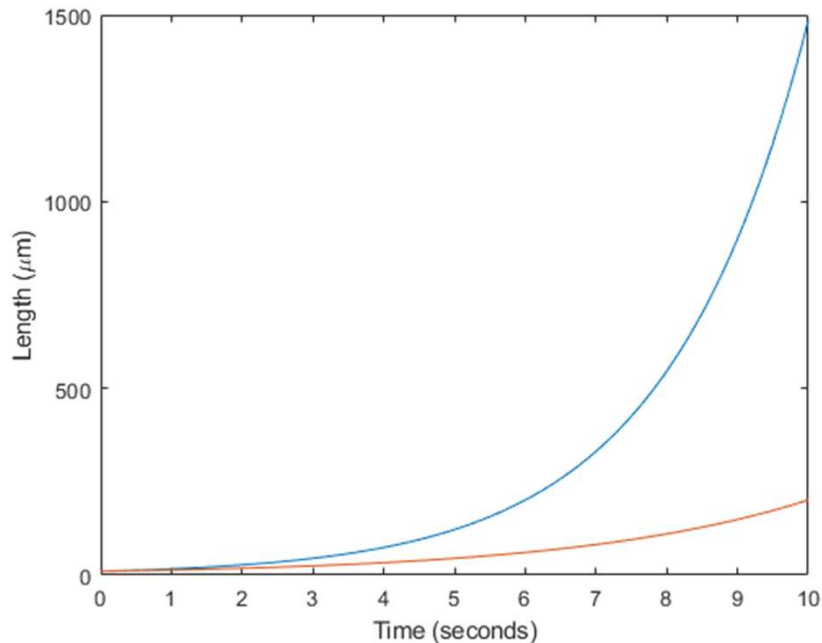
Plotting multiple plots on the same axes

```
plot(xdata1, ydata1, xdata2, ydata2, ...  
     xdataN, ydataN)
```

Modify your script to plot

$$y = 10e^{0.5x}$$

$$y2 = 10e^{0.3x}$$



Example code

```
xx = linspace(0, 10, 100);  
yy = 10 * exp(0.5 * xx);  
  
yy2 = 10 * exp(0.3 * xx);  
  
plot(xx, yy, xx, yy2)  
xlabel('Time (seconds)');  
ylabel('Length (\mum)');  
xlim([0, 2])  
ylim([0, 40])
```


Line specifications

- You can add additional options to change line color and line style etc

```
plot(xx, yy, '--r', xx, yy2, 'ok')
```

Line Specification	Type
' - '	Solid line (default)
' - - '	Dashed line
' . '	Dotted line
' . - '	Dot-dashed line
' o '	Circles

Color Specification	Type
' r '	Red
' g '	Green
' b '	Blue
' y '	Yellow
' k '	Black

* Look up documentation for more examples

Plotting multiple plots on the same axes

- Use 'hold on' and 'hold off'
- Useful when you do not have the data ahead of time

```
figure;  
plot(xx, yy)  
hold on  
plot(xx, yy2)  
hold off
```

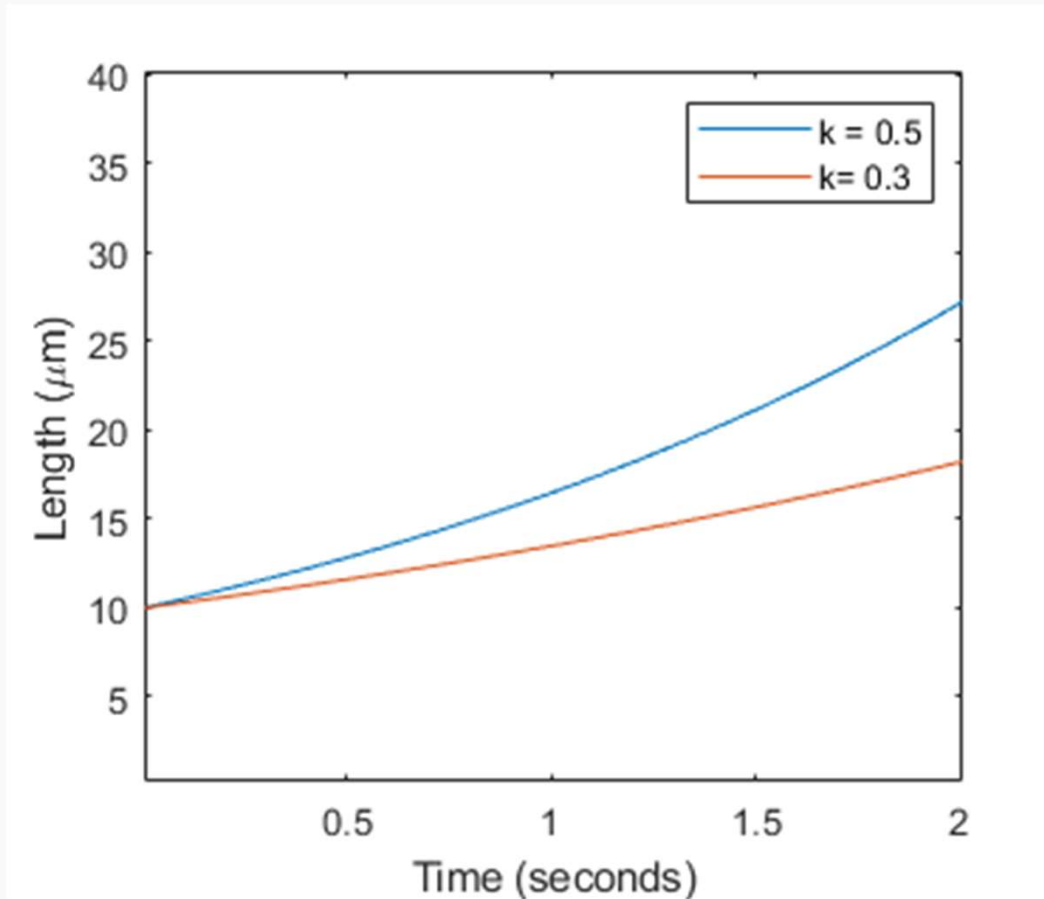
Remember hold off otherwise MATLAB will keep drawing on the same axes

Inserting legends

Example: `legend('k = 0.5', 'k= 0.3')`

Legend for first plot

Legend for second plot



Semilog plots

- Syntax:

```
semilogx(xdata, ydata)
```

```
semilogy(xdata, ydata)
```

Semilog plots only one of the axes using a log scale

Which of the following semilog plots would show the equation below as a straight line?

$$y = 10e^{0.5x}$$

- (A) `semilogx(xdata, ydata)`
- (B) `semilogy(xdata, ydata)`

Example

- Modify your script to make create a new figure window:

```
figure;
```

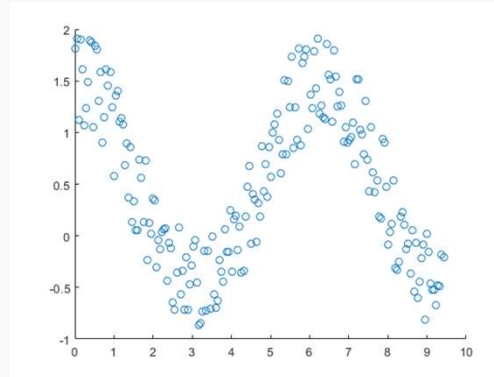
- Plot the data using an appropriate semilog plot so the graph appears as a straight line

```
semilogy(xx, yy)
```

Other plots you might find useful

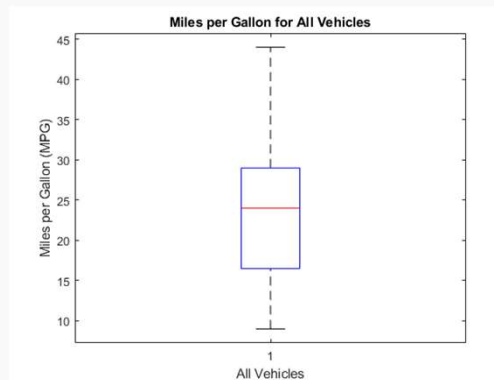
Scatter plot

```
scatter(xdata, ydata)
```



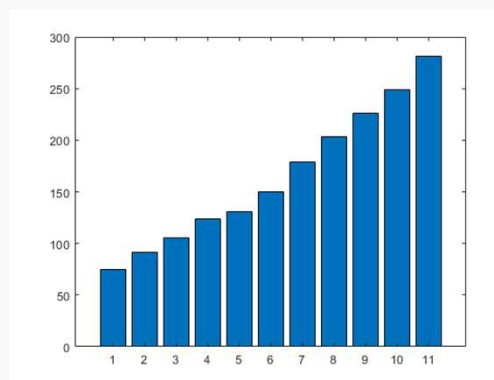
Box-and-whisker plot

```
boxplot(xdata)
```



Bar plot

```
bar(xdata, ydata)
```



Curve fitting

- Curve fitting is a very important tool in data analysis
- It allows you to fit data to a model (a mathematical function that describes the data)

Examples of when you might want to do this in cell microscopy

- Measuring the growth rate of cells – exponential growth
- Measuring size of particles/puncta – Gaussian

There will be some homework questions on these

Basic fitting function

- Syntax:

$$F\theta = \text{fit}(X, Y, FT)$$

Input arguments:

$X, Y =$ **COLUMN vectors** containing data to fit to

$FT =$ String describing model to fit

Output argument:

$F\theta =$ Fit object

Finding the list of fit types

Easiest way:

```
>> doc fit
```

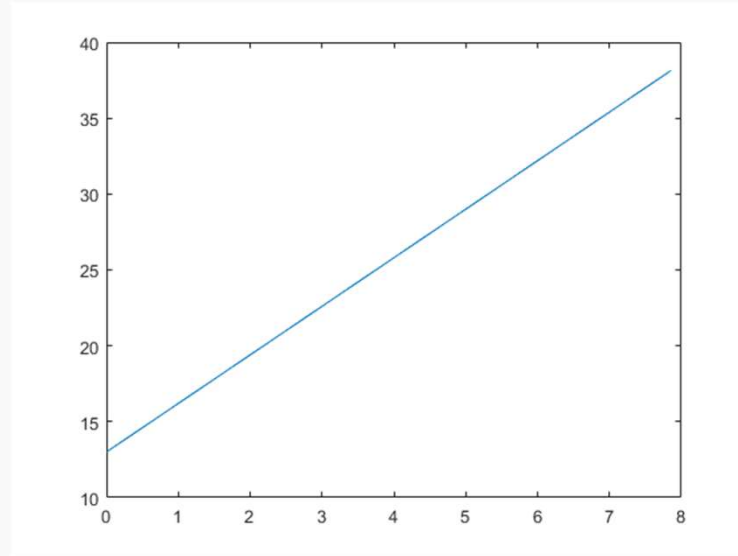
- Scroll to the end, and select

"List of Library Models for Curve and Surface Fitting"

- Link:

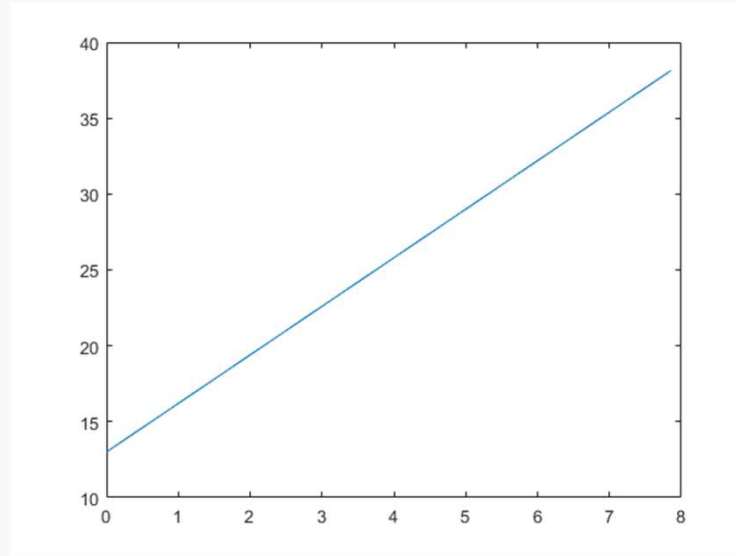
<https://www.mathworks.com/help/curvefit/list-of-library-models-for-curve-and-surface-fitting.html>

What function is most appropriate to fit the following data?



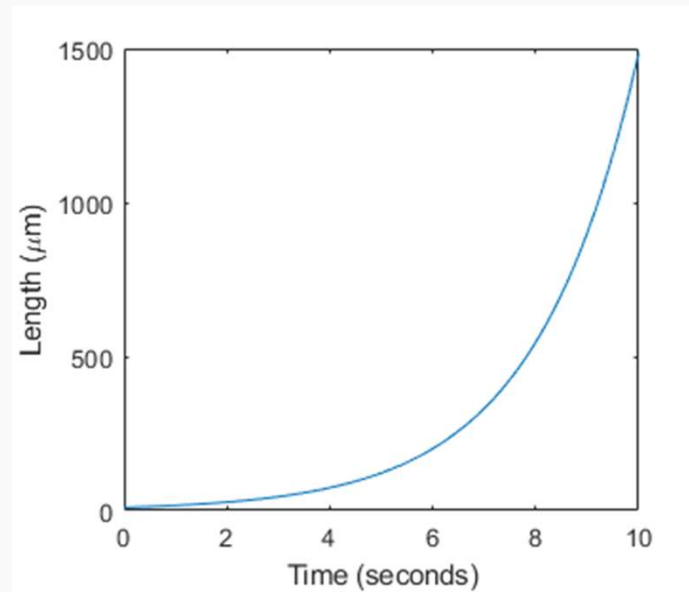
- (A) poly1
- (B) poly2
- (C) gauss2
- (D) sin1

What function is most appropriate to fit the following data?



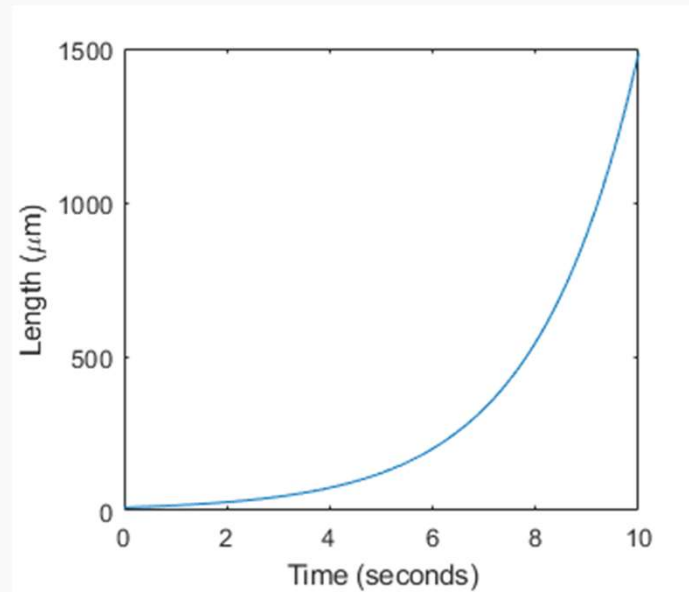
- (A) **poly1**
- (B) poly2
- (C) gauss2
- (D) sin1

What model is most appropriate to fit the following data?



- (A) poly2
- (B) gauss1
- (C) exp1
- (D) exp2

What model is most appropriate to fit the following data?



- (A) poly2
- (B) gauss1
- (C) exp1**
- (D) exp2

Example

- Edit your script to fit the original curve `yy`

`F0 = fit(X, Y, FT)`

Input arguments:

`X, Y` = COLUMN vectors containing data to fit to

`FT` = String describing model to fit

Output argument:

`F0` = Fit object

Example

- Going back to your script, fit a function to the yy data

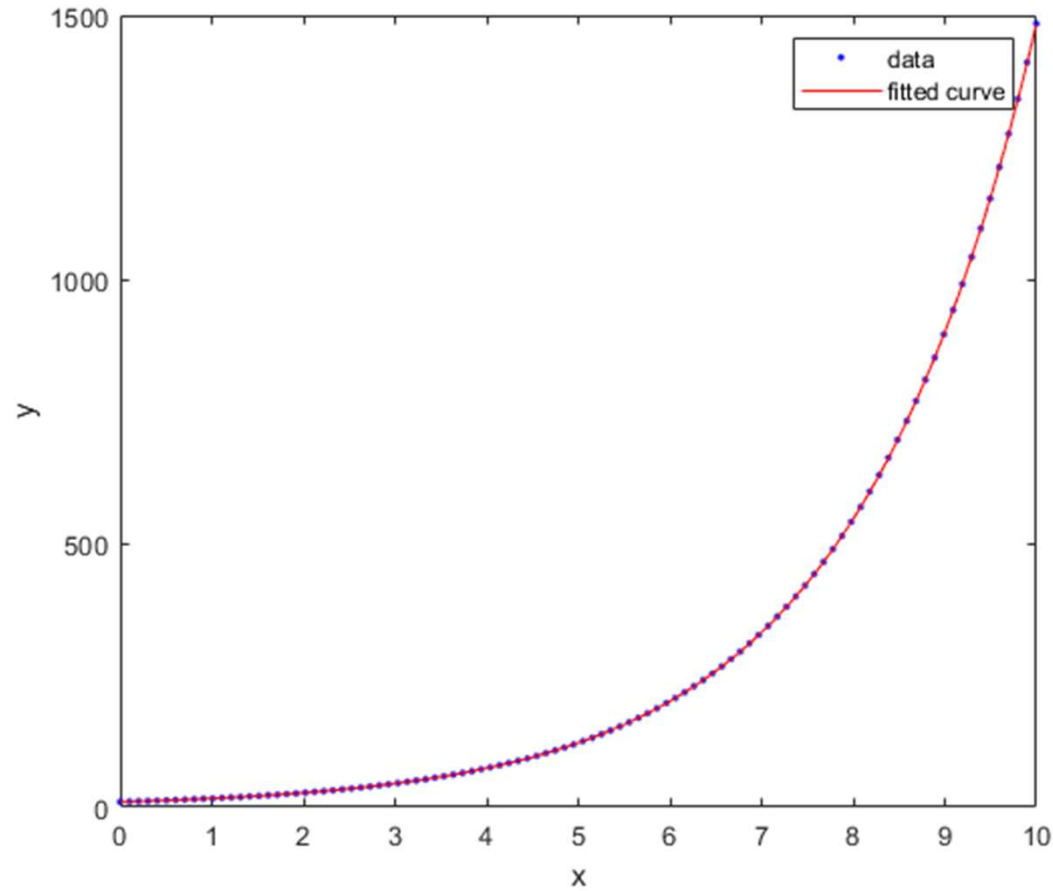
```
fitObj = fit(xx', yy', 'exp1')
```

- Plot the result

```
plot(fitObj, xx, yy)
```

- Pay attention to the order of the arguments
- The first argument is the fit object → this is a special plot

Plotting the fitted data



Be sure to check your fit!

What is the growth rate/growth constant of the curve?

```
>> fitObj
```

```
General model Exp1:
```

```
fitObj(x) = a*exp(b*x)
```

```
Coefficients (with 95% confidence bounds):
```

```
a =          10 (10, 10)
```

```
b =          0.5 (0.5, 0.5)
```

What is the growth rate/growth constant of the curve?

```
>> fitObj
```

```
General model Exp1:
```

```
fitObj(x) = a*exp(b*x)
```

```
Coefficients (with 95% confidence bounds):
```

```
  a =          10  (10, 10)
```

```
  b =          0.5  (0.5, 0.5)
```

```
>> fitObj.b
```

```
ans =
```

```
 0.5000
```

Goodness-of-fit

- Values that statistically describe how well the data fits to the model

```
[fitObj, gof] = fit(xx', yy', 'exp1')
```

- gof is a struct that has five different fields
- The statistic we will use for this course is

rsquare – coefficient of determination

Details about the others:

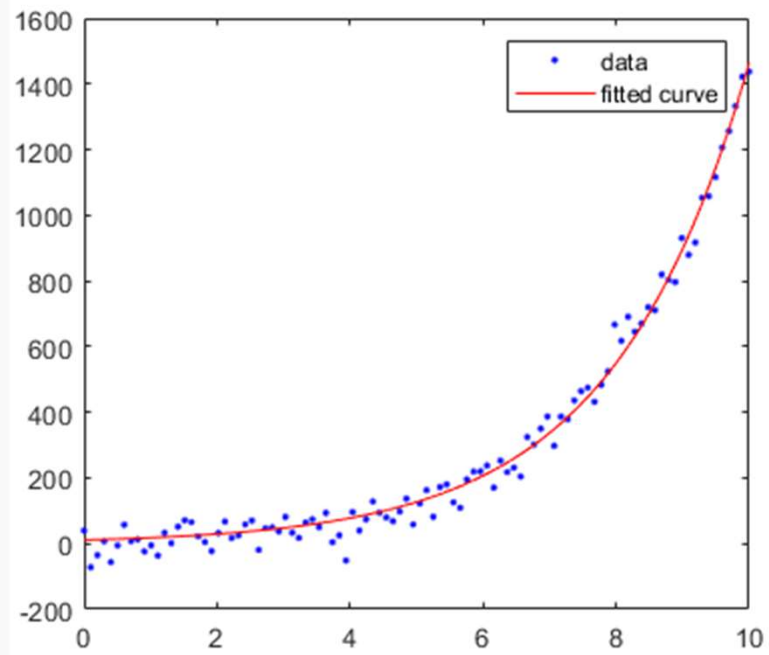
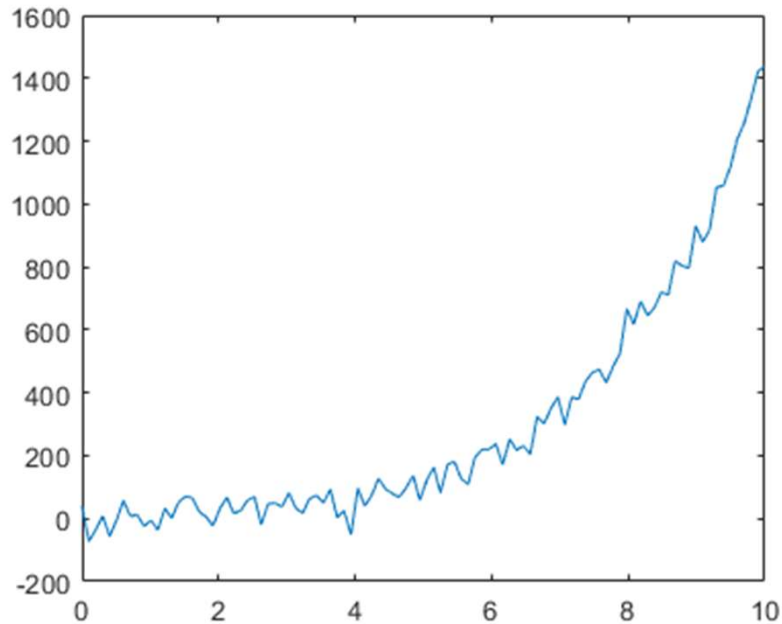
<https://www.mathworks.com/help/curvefit/evaluating-goodness-of-fit.html>

R-squared or the coefficient of determination

- Simple explanation of R^2 is for a measure of the difference of the data from the model
- R^2 typically takes values between 0 and 1
 - $R^2 = 0$ – no data lies on the line described by the model ("bad fit")
 - $R^2 = 1$ – all the data lies on the line described by the model ("perfect fit")
- Typically want values – 0.98 and above
- Beyond the scope of this class, but just be aware that R^2 might not always be the best indicator of goodness-of-fit

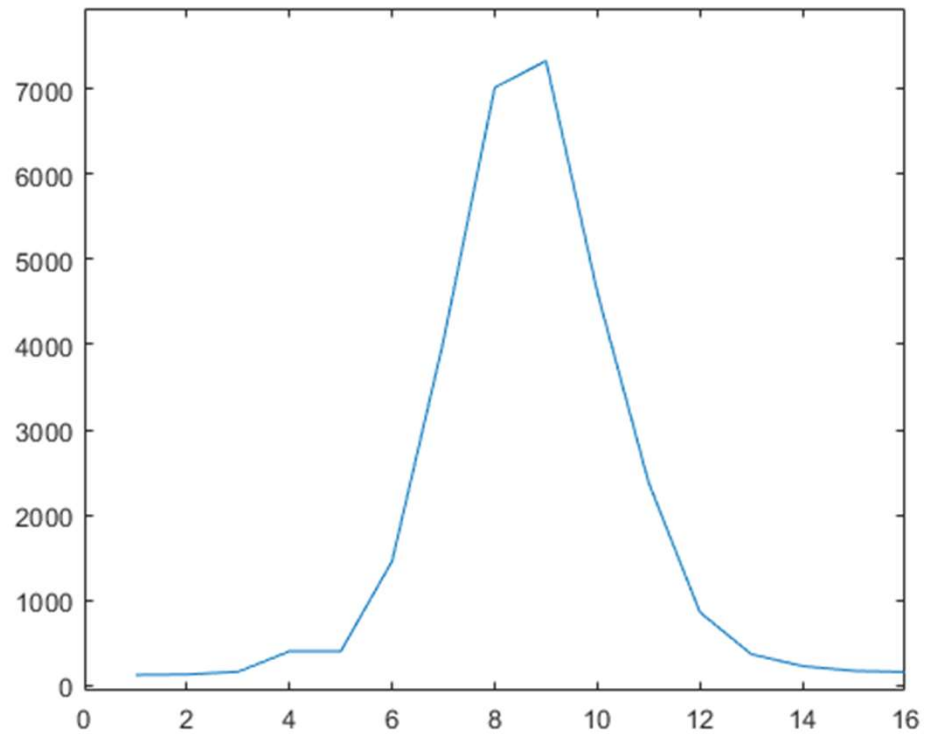
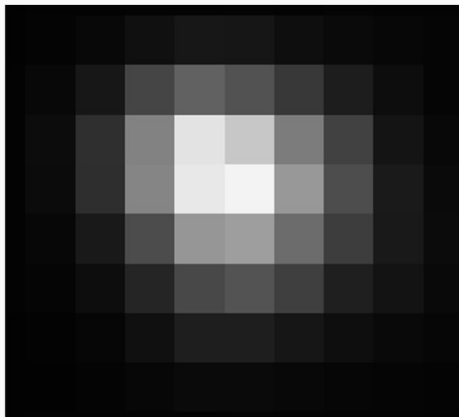
Issues that could affect fitting results

- Noisy images/noisy signals – try median/Gaussian filtering
- Small variations during segmentation – try smoothing (function smooth)

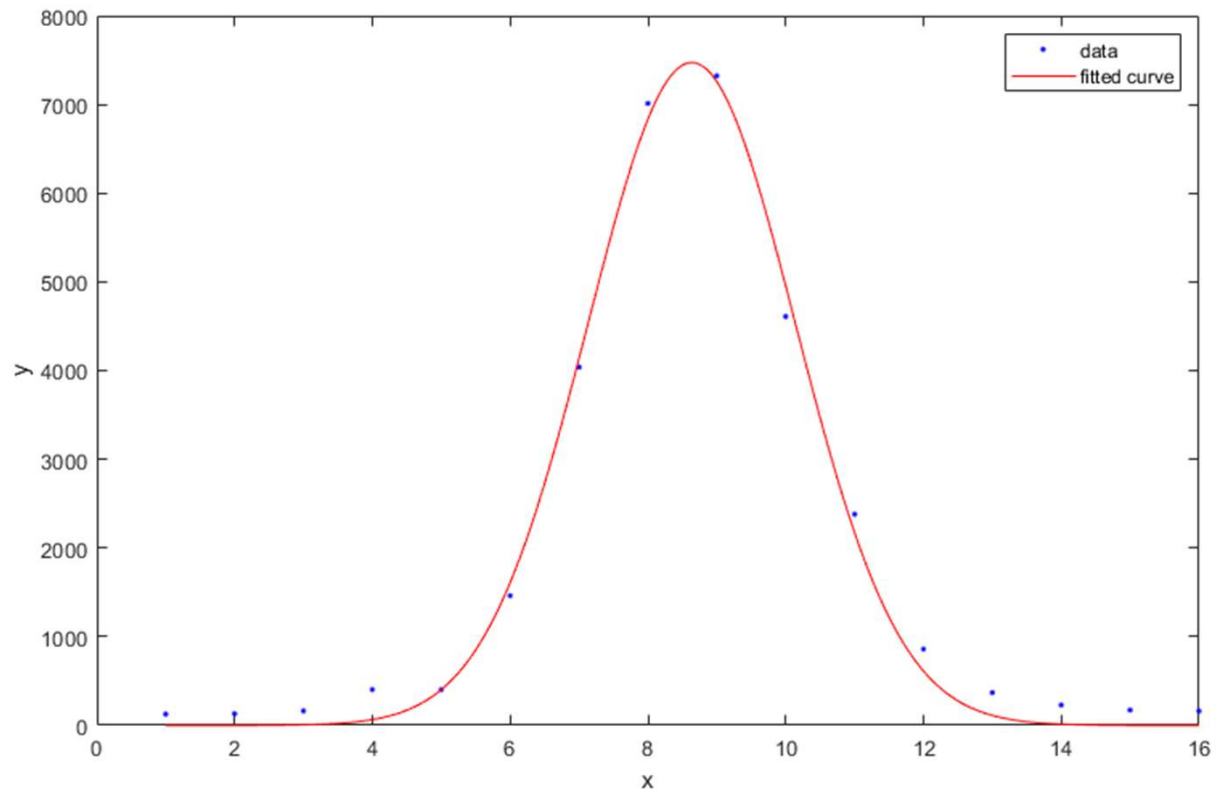


Issues that could affect fitting results

- Constant background illumination/camera dark noise – imaging issue



Inaccurate fitting due to offset



The model 'gauss1' does not have a term for a constant offset

Have to subtract the offset to get a proper fit

Final tips

- Read the documentation/Check the model equations very carefully
- Some equations are a little bit different – there are small variations to general equations depending on its use
 - There is an example of this in your homework
- If unsure what the function looks like, plot it out